

Start here for

Question Number: **8**

$$a) \frac{dP}{dt} = kP$$

$$\int kP \, dP$$

$$= kP^2$$

$$P^2 = k(t) \quad \text{or} \quad P = \sqrt{k(t)}$$

~~$$P^2 = k(t)$$~~

$$b) P(\text{both coins land showing tails}) = 1 - 0.36$$

$$= 0.64$$

$$c) i) A = 4$$

$$y = 4 \sin bx$$

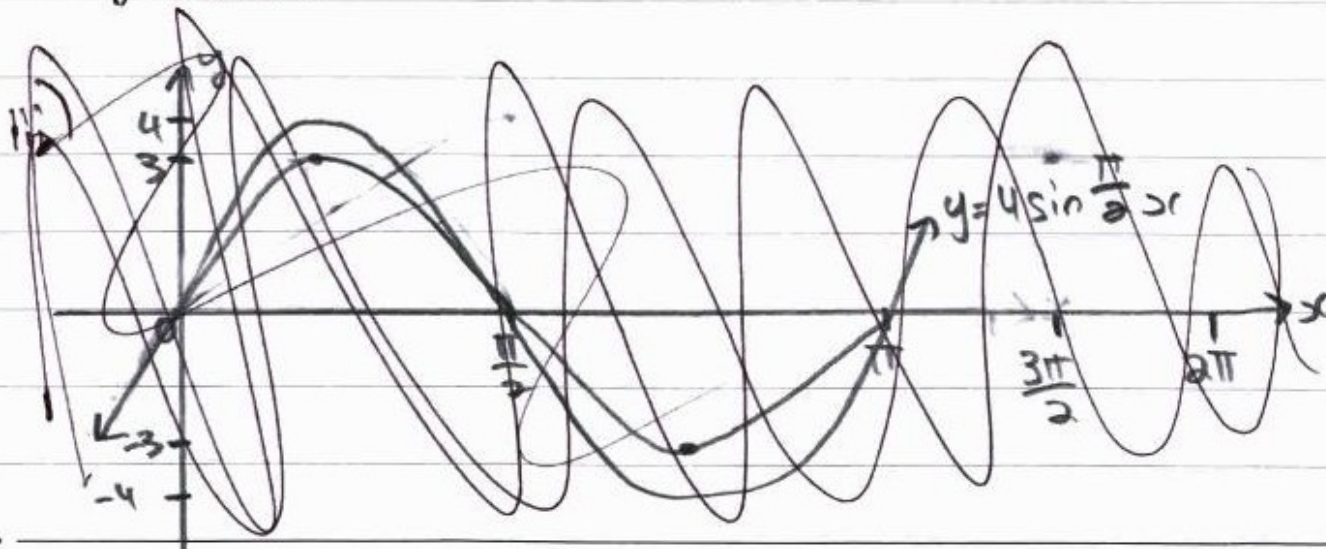
$$ii) b = 4$$

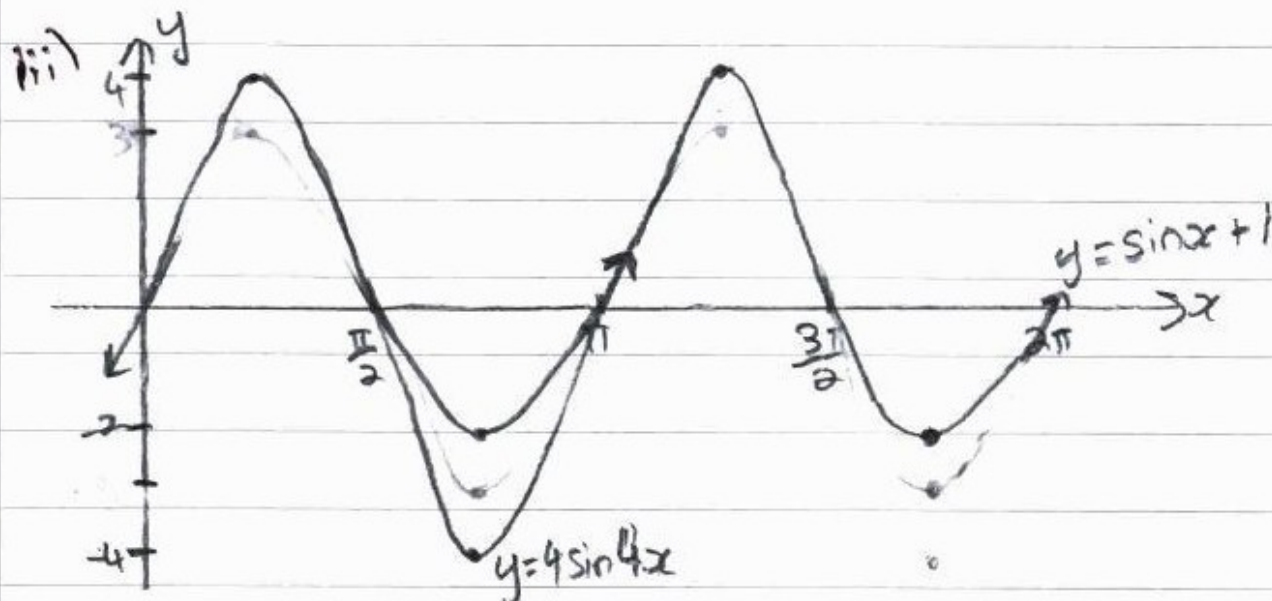
$$\frac{2\pi}{n} = \frac{\pi}{2}$$

$$\frac{4\pi}{\pi} = n$$

$$n = 4$$

$$y = 4 \sin 4x$$





d) $f(x) = x^3 - 3x^2 + kx + 8$

$$f'(x) = 3x^2 - 6x + k$$

$$f''(x) = 6x - 6$$

$$0 > 6x - 6$$

$$3 > 6x$$

$$\frac{1}{2} > x$$

$$f(x) = x^3 - 3x^2 + kx + 8$$

$$0 = \left(\frac{1}{2}\right)^3 - 3\left(\frac{1}{2}\right)^2 + k\left(\frac{1}{2}\right) + 8$$

$$= \frac{1}{8} + 2.25 + \frac{1}{2}k + 8$$

$$= 10.375 + \frac{1}{2}k$$

$$-10.375 = \frac{1}{2}k$$

$k = -20.75$ where $f(x)$ is an increasing function.

Additional writing space on back page.