

**Question 6** (12 marks) Use a SEPARATE writing booklet.

(a) Sketch the graph of  $y = \sqrt{4 - x^2}$ , and state the range. 2

(b) The gradient function of a curve is given by

$$f'(x) = 3(x + 1)(x - 3)$$

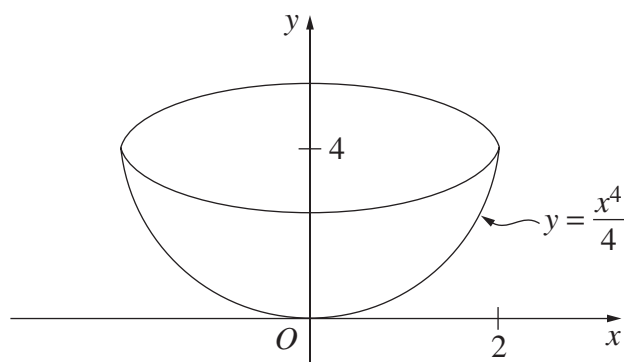
and the curve  $y = f(x)$  passes through the point (0, 12).

(i) Find the equation of the curve  $y = f(x)$ . 2

(ii) Sketch the curve  $y = f(x)$ , clearly labelling turning points and the y intercept. 3

(iii) For what values of  $x$  is the curve concave up? 1

(c) 4



A bowl is formed by rotating the part of the curve  $y = \frac{x^4}{4}$  between  $x = 0$  and  $x = 2$  about the  $y$  axis.

Find the volume of the bowl.